

# Dynamic-Stochastic Influence Diagrams: Integrating Time-Slices IDs and Discrete Event Systems Modeling

Xin Zhao, Yin-fan Zhu, Wei-ping Wang, and Qun Li

**Abstract**—The Influence Diagrams (IDs) is a kind of Probabilistic Belief Networks for graphic modeling. The usage of IDs can improve the communication among field experts, modelers, and decision makers, by showing the issue frame discussed from a high-level point of view. This paper enhances the Time-Sliced Influence Diagrams (TSIDs, or called Dynamic IDs) based formalism from a Discrete Event Systems Modeling and Simulation (DES M&S) perspective, for Exploring Analysis (EA) modeling. The enhancements enable a modeler to specify times occurred of endogenous events dynamically with stochastic sampling as model running and to describe the inter-influences among them with variable nodes in a dynamic situation that the existing TSIDs fails to capture. The new class of model is named Dynamic-Stochastic Influence Diagrams (DSIDs). The paper includes a description of the modeling formalism and the hierarchy simulators implementing its simulation algorithm, and shows a case study to illustrate its enhancements.

**Keywords**—time-sliced influence diagrams; discrete event systems; dynamic-stochastic influence diagrams; modeling formalism; simulation algorithm

## I. INTRODUCTION

THE weapon and equipment system of systems (SoS) demonstration is a high level complex systems analysis issue and involves vast uncertain factors. In the modern complex world, decision makers are faced with an ever increasing number of situations that require a all-around response, ranging from terrorisms to local battles and perhaps campaign between multi-national organizations for the employment of military forces to achieve or maintain demonstration objectives. To handle them effectively, Rand has gave a Exploring Analysis (EA)[1] methodology for Capabilities-Based Planning (CBP)[2][3]. As a model-based method, EA needs suitable model form for analysis supporting. The model's characters include: lower resolution; reflecting cause and effect relationship clearly; running promptly; less parameters; and could covering enough issue scope.

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The extended Time-Sliced Influence Diagrams (TSIDs) [5][6] allows the existence of dynamic feedback loop circle to classic IDs[7] for graphic modeling. It's a special instance of Dynamic Bayesian Networks (DBNs) [8][9], that increases the decision nodes and the objective nodes for optimization of decision-making, not just probabilistic evaluation only. The TSIDs allows a system analyst to observe how uncertainties of variables influence model's behavior with time changing. TSIDs had been experimentally used in the area of EA for describing important factors of campaign and their relationships dynamically [10][11]. The TSIDs-based formalism is appropriate to answer influences queries and to perform what-if analyses.

Despite its ability to model complex situations in a compact and easy to read manner, TSIDs fails to capture variance of time sequences among events of dynamic situations. Furthermore, from another view, the object that TSIDs could describe is usual an independent process or subpart of the high-level process. This is its inherent deficiency for complex cooperated processes description.

In other words, although TSIDs connects 'uncertainty' with 'time' by a time-slice concept, it still can't be fit for all kinds of high level modeling. If the 'system' not only has complex entities but also complex relationships, it's not easy to reflect its process clear. Take military campaign for example, if it contains interactional crossed loops that caused by different weapons and troops, it's hard to abstract them.

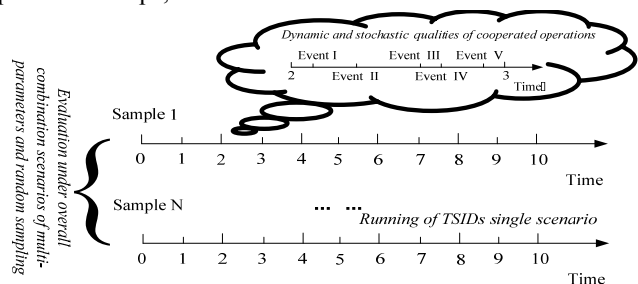


Fig. 1 Temporal Sequence of TSIDs

Moreover, the relationship description between times or influence factors are settled in TSIDs. It's not enough to describe the dynamic and stochastic cooperated operations. As Fig.1, TSIDs just runs short of variational temporal sequences among different time-slices.

This shortcoming of TSIDs may turn out to be unrealistic in

many real world situations. The paper proposes syntax and semantic enhancement to TSIDs to overcome the limitation. The enhancement would enable a system analyst to model the impacts of different actions on the desired effect in a dynamic uncertain situation.

The rest of the paper is organized as follows. Section II describes the technical background-IDs, TSIDs, and the combination for TSIDs and DES. Sections III and IV describe the proposed modeling formalism and its simulation algorithm, respectively. Section V illustrates the proposed enhancements by a case study that realized in EASim-an IDs modeling tool. Finally, Section VI concludes the paper and points towards the future research direction.

## II. TECHNICAL BACKGROUND

### A. Classic IDs

Classic Influence Diagrams (IDs) [7] is a directional acyclic graph for decision-making issue modeling. It's also a probability net being used for solving uncertainty and reflecting qualitative & quantitative knowledge synthetically and an effective tool for information communication. Decision-making analysis based on IDs is usual at strategic level. The classic IDs is formed by directional arcs and nodes with data structures, as Fig.2.

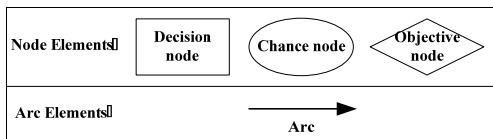


Fig. 2 Graphical elements of classic IDs

The developing process of IDs is field and application oriented basically. Their evolvement separately or simultaneously occurred at relation, function and value level, including[12][13][14][15][16][17][18]: Probability IDs, Fuzzy IDs, Rough IDs, Potential IDs, Monotonic IDs and Ignorant IDs etc. No matter what requirements of application they fulfilled or what levels they occurred at, the essential purpose is to utilize the IDs' powerful abilities to graphically capture causal and influence relationships for analytical modeling that is a kind of methodology for analyzing complex strategic decision-making issue. Among them, Time-Sliced IDs (TSIDs) is especially worthy to get attention for model-based high level issue decision-making analysis.

### B. Time-Sliced IDs

By introducing time concept and dynamic character, TSIDs extended classic IDs and could support differential equation and continue system modeling for analysis. This also made it more fit for abstracting averaged process, and improved cause and effect influence net's description comparing with static analytic IDs, as Fig.3.

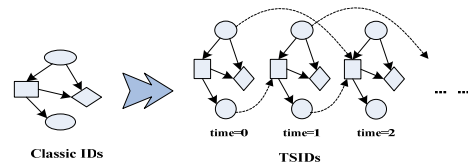


Fig. 3 Classic IDs to TSIDs

An TSIDs is a four-tuple  $TSIDs = \langle D, M, A, h_N \rangle$  where

- ◆  $D$  is the index set of nodes;
- ◆  $M = \{M_d \mid d \in D\}$  is the set of variable nodes;
- ◆  $A$  is the set of influence arcs;
- ◆  $h_N$  is the iterative step.

### C. Combination of TSIDs and DES M&S

The capability to enhance that TSIDs needs is just what the Discrete Event Systems (DES) M&S owned. DES [19][20][21] can express the input and intrinsic random, time delay, and queue. And so it can describe simultaneous, cooperating and multilevel complex processes. It's a good reference for TSIDs improvement. The combined modeling of TSIDs and DES can form a new formalism to enhance the top-down complex system modeling. So, when you do a high level complex issue modeling, the TSIDs part can be used to model the issue's macrostructure parts well, and the DES part can be used to model other detailed parts.

1) *Relationship of 'time' conception:* The two parts (TSIDs and DES) should have accordant 'time' conception. So 'Etime' is introduced to represent event time comparing with 'Ftime' that representing feedback time, as Fig.4.

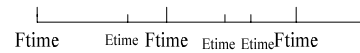


Fig. 4 Event time and feedback time

2) *Combination mode:* From the graphic syntax and semantic point of view, the nodes in DES M&S must have bidirectional relationship with the variables of TSIDs, whether events, states, activities, or processes they figured. Considering discrepancies of two parts, their elements may have two kinds of combination modes: one is node-combined, what need holistic simulated evaluation, and is a multi-granularity description to the same level and towards behavior (event) principally; the other is module-combined, what need separated simulated evaluation, and is a multi-resolution description to different levels and towards entity principally. The former mode is flexible and suit for complex system description especially to our situation.

3) *Principles:* As amelioration to existing method, it just should

- ◆ Be graphic, and needs less extension to TSIDs;
- ◆ Be intuitionist;
- ◆ Be prone to understand, and be convenient for model structure redress and relationship explanation;
- ◆ Unitive rule, and be convenient for software design and implementation.

### III. PROPOSED MODELING FORMALISM

In this paper, the improved method is called as ‘Dynamic-Stochastic Influence Diagrams (DSIDs)’, for its ability for dynamic arranging of stochastic events, processes and influences, and supporting their random treating. To describe the characters of DES, DSIDs add a ‘Time node’ at TSIDs foundation, expressing stochastic events by time list directly, as Fig.5. This is propitious to assort with nodes of TSIDs, and to transfer evaluating engine.

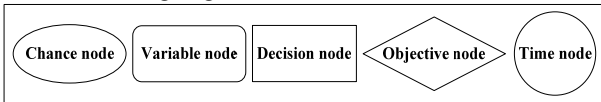


Fig. 5 Primary variable nodes of DSIDs

The DSIDs describes pivotal elements of issue by these graphic nodes, and the connection of them form a DSIDs net model. In addition, as a graphic modeling method, it should be considered that doing some structural processing for input and output interfaces during the description of DSIDs formalism. A standard DSIDs model specification is a structure:

$$DSIDs = \langle D, M, A, I, Z, h_N, t, ta \rangle$$

Where

- ◆  $D$  is the index set of nodes;
- ◆  $M = \{M_d \mid d \in D\}$  is the set of variable nodes;
- ◆  $A$  is the set of influence arcs;
- ◆  $I = \{I_d \mid d \in D\}$  is the set of nodes that influence node  $M_d$ ;
- ◆  $Z = \{Z_d \mid d \in D\}$  is the interface mapping set of node  $M_d$ ;
- ◆  $h_N$  is the iterative step;
- ◆  $t$  is the current time;
- ◆  $ta$  is the time advance function.

#### A. Nodes Set

There are five kinds of nodes in DSIDs,  $M = N_C \cup N_V \cup N_D \cup N_O \cup N_T$  namely chance node, variable node, decision node, objective node, and time node. Hereinto, the variable form of time node is chain list for value storage representing the time that event will take place.

To  $\forall d \in D$ ,  $M_d = \langle n, X_d, Y_d, V_{init}, V_d, \Delta_d, \Lambda_d, t, h \rangle$ , in which

- ◆  $n \in NP$  is the name of node, and  $NP$  is the name space;
- ◆  $t$  is the current time;
- ◆  $h$  is the current actual step;
- ◆  $V_{init}$  is the initialized value, maybe a number or a depending function to other nodes;
- ◆  $V_d$  is the value of node to each time;
- ◆  $X_d = \{(p, v) \mid p \in IPorts_d, v \in X_{p_d}\}$  is the multivariable set of inputs of the node with  $IPorts_d$ ;
- ◆  $Y_d = \{(p, v) \mid p \in OPorts_d, v \in Y_{p_d}\}$  is the multivariable set of outputs of the node with  $OPorts_d$ ;
- ◆  $\Delta_d$  is the internal logic function;

- ◆  $\Lambda_d$  is the output mapping function.

Of course, to different nodes, the detailed definitions are different that be omitted for conciseness here.

The semantic executing of node can be described as follow: After computed the time advanced by node net (DSIDs), nodes receive the value of  $t$  and  $h$ ; when received the value  $X_{d(t)}$  from all input ports, based on themselves' forepassed value, them transact internal logic by  $\Delta_d$ , calculate output values by  $\Lambda_d$  and map them to output ports.

#### B. Arcs Set

The influence relationships are figured by arcs in DSIDs and different for the sort of nodes they connected, to form the net structure together with all nodes. In DSIDs,  $A = A_R \cup A_I \cup A_E \cup A_F \cup A_C \cup A_A$ , as Tab.I.

The former four are the same as those of TSIDs, and the later

TABLE I  
ARROWS AND THEIR SIGNIFICATION

Arc	Definition	Signification
$A_R$	$\{(x, y), x \in N_C \cup N_V, y \in N_V \cup N_O\}$	relevancy
$A_I$	$\{(x, y), x \in N_C \cup N_V, y \in N_D\}$	information
$A_E$	$\{(x, y), x \in N_D, y \in N_V \cup N_O\}$	influence
$A_F$	$\{(x, y), x \in N_D, y \in N_D\}$	order
$A_C$	$\{(x, y), x \in N_V, y \in N_T\}$	condition
$A_A$	$\{(x, y), x \in N_T, y \in N_V \cup N_T\}$	action

two are what DSIDs has peculiarly. Respectively,  $A_C$  indicates condition that its source node provides to target node, and  $A_A$  indicates action that its source node affects to target node when the event happened.

In addition, there is also a loop restriction in DSIDs as follow: In the net connected by  $A_R, A_I, A_E, A_F$  and correlative nodes, there couldn't exist circle depending that without time delay. Namely, to  $\forall i, j \in D$ , if the calculation of  $V_{i(t)}$  indirectly depends on  $V_{j(t)}$ , then the calculation of  $V_{j(t)}$  couldn't depends on  $V_{i(t)}$  synchronously, no matter directly or indirectly.

#### C. Other Constituents

1) The set of nodes that influence  $M_d$  :

To  $\forall d \in D: I_d = \{i \mid ((i, fromport), (d, toport)) \in IC\}$ , where  $IC \subseteq \{((a, op_a), (b, ip_b)) \mid a, b \in D, op_a \in OPorts_a, ip_b \in IPorts_b\}$  that expressing linked relationships.

2) The interface mapping set of  $M_d$  : To  $\forall d \in D: Z_d = \times_{i \in I_d} Y_i \rightarrow X_d$ ,  $Z_d(\dots, Y_{(i, fromport)}, \dots) = X_{(d, toport)}$ , and

$$x_{(d, toport)} = \bigoplus_{\{(i, fromport) \mid ((i, fromport), (d, toport)) \in IC\}} y_{(i, fromport)}$$

Where  $\bigoplus x = x$ ; if  $x_i \neq \emptyset \wedge \forall j \neq i \Rightarrow x_j = \emptyset$ , then  $\bigoplus x_1, x_2, \dots, x_n = x_i$ , else  $\bigoplus x_1, x_2, \dots, x_n = \emptyset$ . '  $\bigoplus$  ' allow

several output ports linked to one input port. It's helpful to DES expression [21].

3)  $t$  and  $h_N$ :  $t$  is the current time,  $h_N$  corresponds to the 'Ftime' conception that mentioned before, they are calculated by function 'ta'.

4) *Time advance function 'ta'*: The time-advance of DSIDs needs to consider time values updating and events arising. This situation is similar to multiformalism M&S of discrete time and discrete event systems. There is a similar concept 'state event[21]' too. The implementation of function  $ta$  followed the 'bisection method' arithmetic that the article [21] mentioned. It's the function of  $t$ ,  $h_N$  and  $V_d$  of all nodes, and so

$$ta : \times_{d \in D} V_{d(t)} \times t \times h_N \rightarrow R_{0, \infty}^+$$

IV. SIMULATION ALGORITHM FOR DSIDs EVALUATION

The algorithm of DSIDs simulated evaluation could be described as Fig.6. To see the detail of TSIDs evaluation algorithm implementation, you may take [5][6][9][22] for references. The algorithm and the 'forward calculate' will be materialized in the description of simulators next.

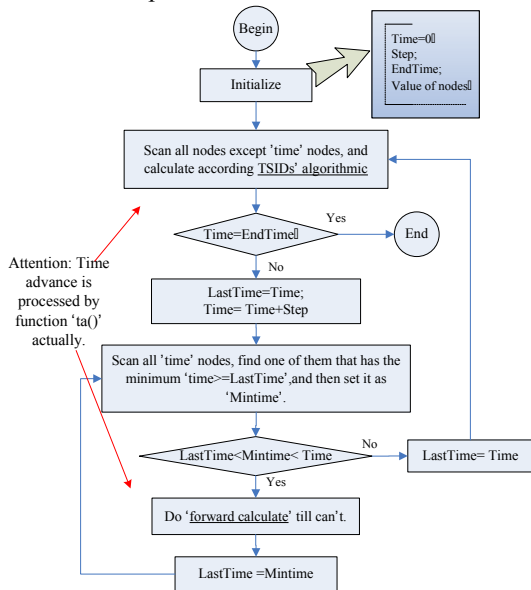


Fig. 6 The logistic process of DSIDs evaluation algorithm

The 'LastTime' of algorithm expresses the latest calculating time that between 'Time' and 'Time-Step' (Step=1 here), as Fig.7.

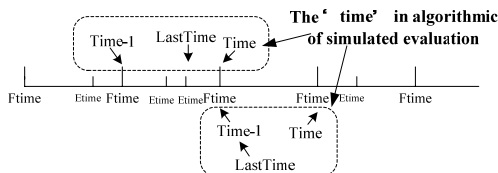


Fig. 7 The 'time' in evaluation processing

The algorithm is compatible for TSIDs, and so they (TSIDs & DSIDs) are equivalent without 'time node'.

A. Hierarchy

The simulators of DSIDs may have clear hierarchy as Fig.8. The DSIDs simulator structure is compartmentalized into 'node-simulator' for 'node' and 'net-coordinator' for 'net' that formed by nodes. The former control the operation of nodes, and the later define the connection of them. Moreover, 'net-coordinator' also takes charge for time advancing, state events scheduling, and messages transferring etc. In addition, a 'root-simulator' is introduced to control simulation repetition which will not be discussed detailed in this paper.

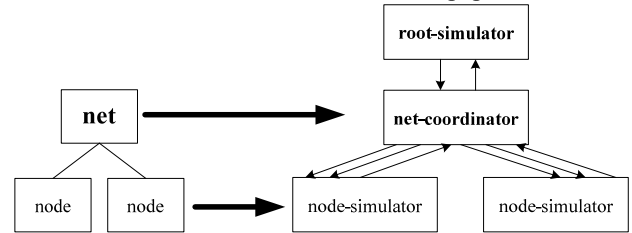


Fig. 8 Hierarchy of DSIDs simulators

The simulation algorithm of DSIDs is implemented based on the following seven kinds of messages. DSIDs scheduling process is realized by messages communication.

TABLE II  
SEVEN KINDS OF MESSAGES IN COMMUNICATION

Name	Message	Send and Receive
$i$	Initialization	upper to lower
*	Calculation enabled	net-coordinator to node-simulator
$e$	Event schedule	net-coordinator to node-simulator of $N_T$
$r$	Earliest time of the future event	node-simulator of $N_T$ to net-coordinator
$se$	Failure of state event	node-simulator of $N_T$ to net-coordinator
$x$	Value input	net-coordinator to node-simulator
$y$	Value output	node-simulator to net-coordinator

Tab.II shows symbols of seven messages on which the DSIDs evaluation is based, while their sending and receiving mode are described in Tab.III.

TABLE III  
MESSAGE SEND AND RECEIVE FOR EACH SIMULATOR

Message	node-simulator					net-coordinator	root-simulator
	$N_C$	$N_V$	$N_D$	$N_O$	$N_T$		
$(i, t)$	↓	↓	↓	↓	↓	↓→	→
$(* , t)$	↓	↓	↓	↓	↓	↓→	--
$(e, t)$	--	--	--	--	↓	→	--
$(r, t)$	--	--	--	--	→	↓	--
$(se, t)$	--	--	--	--	→	↓	--
$(x, t)$	--	↓	↓	↓	↓	→	--
$(y, t)$	→	→	→	--	→	↓	--

Legends: ↓ : receive; → : send; --: void.

B. Description of Simulators

The following sections will show detail of algorithm realization for each simulator.

1) *Node-Simulator*: There are four node-simulators for different kinds of nodes. They all base on the basic

node-simulator and have each peculiarity. Fig.9 to Fig.14 shows details.

```

basic - node - simulator for  $M_d$ 
variab les :
    parent // net - coordinato r
    tl // time of last
    tn // time of now
     $M_d = \langle n, X_d, Y_d, V_{init}, V_d, \Delta_d, A_d, t, h \rangle$ 
when receive  $i$  - message  $(i, t)$  at time  $t$ 
    tl = t
    tn = t
when receive * - message  $(*, t)$  at time  $t$ 
    if  $t \leq tn$  then
        error : bad synchroniz ation
when receive  $e$  - message  $(e, t)$  at time  $t$ 
    if  $t \leq tn$  then
        error : bad synchroniz ation
when receive  $x$  - message  $(x, t)$  at time  $t$ 
    //wi th input valu e  $x_{(r,toport)}$  =
    //  $Z_{(d^*,frompo rt),(r,top ort)}(y_{(d^*,frompo rt)})$ 
    if  $t \leq tn$  then
        error : bad synchroniz ation
end basic - node - simulator
    
```

Fig. 9 Modality of basic node-simulator

```

node - simulator for  $n \in N_C$ 
when receive * - message  $(*, t)$  at time  $t$ 
    if  $Y_d = \emptyset$  then
        error : bad synchroniz ation
     $Y_d = V_{d(t)} = \Delta_d(t, h)$ 
    send  $y$  - message  $(y, t)$  to parent
    tl = tn
    tn = t
end node - simulator
    
```

Fig. 10 Node-simulator for chance node

```

node - simulator for  $n \in N_D$ 
when receive * - message  $(*, t)$  at time  $t$ 
    if  $Y_d = \emptyset$  then
        error : bad synchroniz ation
    if  $X_d = \emptyset$  then
         $Y_d = V_{d(t)} = \Delta_d(t, h, V_d)$ 
        send  $y$  - message  $(Y_d, t)$  to parent
        tl = tn
        tn = t
when receive  $x$  - message  $(x, t)$  at time  $t$ 
     $x_{(d,toport)(t)} = x_{(r,toport)}$ 
    if  $Y_d = \emptyset$  then
        error : bad synchroniz ation
    if  $X_d = \emptyset$  then
        error : bad synchroniz ation
    if  $\exists x_{(d,port)(t)} = \emptyset$  then //  $x_{(d,port)} \in X_d$ 
        do nothing
     $Y_d = V_{d(t)} = \Delta_d(t, h, V_d, X_{d(t)})$ 
    send  $y$  - message  $(Y_d, t)$  to parent
    tl = tn
    tn = t
end node - simulator
    
```

Fig. 11 Node-simulator for decision node

```

node - simulator for  $n \in N_V$ 
when receive  $x$  - message  $(x, t)$  at time  $t$ 
    if  $Y_d = \emptyset$  then
        error : bad synchroniz ation
    if  $X_d = \emptyset$  then
        error : bad synchroniz ation
     $x_{(d,toport)(t)} = x_{(r,toport)}$ 
    if  $\exists x_{(d,port)(t)} = \emptyset$  then //  $x_{(d,port)} \in X_d$ 
        do nothing
     $Y_d = V_{d(t)} = \Delta_d(t, h, V_d, X_{d(t)})$ 
    send  $y$  - message  $(Y_d, t)$  to parent
    tl = tn
    tn = t
end node - simulator
    
```

Fig. 12 Node-simulator for variable node

```

node - simulator for  $n \in N_O$ 
when receive  $x$  - message  $(x, t)$  at time  $t$ 
    if  $Y_d = \emptyset$  then
        error : bad synchroniz ation
    if  $X_d = \emptyset$  then
        error : bad synchroniz ation
     $x_{(d,toport)(t)} = x_{(r,toport)}$ 
    if  $\exists x_{(d,port)(t)} = \emptyset$  then //  $x_{(d,port)} \in X_d$ 
        do nothing
     $V_{d(t)} = \Delta_d(t, h, V_d, X_{d(t)})$ 
    tl = tn
    tn = t
end node - simulator
    
```

Fig. 13 Node-simulator for objective node

```

node - simulator for  $n \in N_T$ 
variab les :
    tle // t ime of last event
     $ar_{int}$  // accurary reached judgement function
     $P$  // priority
     $cancel_{int}$  // cancel event
when receive  $e$  - message  $(e, t)$  at time  $t$ 
    if  $Y_d = \emptyset$  or  $X_d = \emptyset$  then
        error : bad synchroniz ation
    if  $\exists x_{(d^*,port)(t)} = \emptyset$  then
        //  $x_{(d^*,port)} \in X_d \wedge d^* \notin D_{N_T}$ 
        error : bad synchroniz ation
    find earliest t ime  $t_e$  from  $V_d$  //just find it
    if  $t_e > t$  then
        send  $r$  - message  $(t_e, t)$  to parent
        tl = tn
        tn = t
    if  $\Delta_d(t, h, X_{d(t)}) = false$  then //e vent conditions
        send  $r$  - message  $(t_e, t)$  to parent
        tl = tn
        tn = t
    if  $ar_{int}(t_e, t) = false$  then
        send  $se$  - message  $(se, t)$  to parent
    tak e  $t_e$  out from  $V_d$  //take it out
    if  $cancel_{int}(t_e, V_d, t, h, X_{d(t)}) = false$  then
        tle = t
        tl = tn
        tn = t
         $h = tn - tl$ 
         $Y_d = \wedge_d(tle, t, h, X_{d(t)})$ 
        send  $y$  - message  $(Y_d, t)$  to parent
        find earliest t ime  $t_e$  from  $V_d$  //just find it
        send  $r$  - message  $(t_e, t)$  to parent
when receive  $x$  - message  $(x, t)$  at time  $t$ 
    if  $d^* \notin D_{N_T}$  then
         $x_{(d,toport)(t)} = x_{(r,toport)}$ 
        add  $x_{(r,toport)}$  to  $V_d$ 
end node - simulator
    
```

Fig. 14 Node-simulator for time node

What needs to be specially explained is that the simulator for time node: differentiate input values that from  $N_T$  and non- $N_T$ ; includes two special functions,  $ar_{int}(t_e, t)$  for state event accuracy judgment and  $cancel_{int}(t_e, V_d, t, h, X_{d(t)})$  for event canceling; and owns several output ports to drive other time nodes or influence linked variable nodes.

2) *Net-Coordinator*: After the definition of node-simulators, the net-coordinator, whose task is to send and receive messages to make time advanced and nodes calculated, could be discussed. See Fig.15 for details.

```

net - coordinato r
variabl es :
    parent // root - coordinato r
    tl // time of last
    tn // time of now
    tf // time of future (next step time)
    fTime // FTime
    DSIDs =< D,M,A,h_N,ta,I,Z > //net
when receive i - message (i,t) at time t
    for each d in D do
        send i - message( i,t) to child d
    fTime = t
    tl = t
    tn = t
    tf = +∞
    send * - message( *,t) to self
when receive * - message ( *,t)
    whi le t = fTime + h_N do fTime = t
    tl = tn
    tn = t
    tf = +∞
    for each d in D do
        send * - message( *,t) to child d
    loop
    for each d in D_{N_r} do
        send e - message( e,t) to child d
        //accord ing P : priority
    until there wasn' t event occurred
    if tf > fTime + h_N then
        tf = fTime + h_N
        send * - message( *,tf) to self
        send * - message( *,tf) to self
when receive r - message (r,t) at time t
    if tn < r < tf then
        tf = r
when receive se - message (se,t) at time t
    stop the computatio n of all children
    rollback all variables and events to time = tl
    tf = (tf-tn)/ 2 // ta algorithm
    send * -message( *,tf) to self
when receive y - message (y,t) from d*
    //with output val ue y_{(d^*,frompo rt)}
    receivers = {(r,toport ) | r ∈ D}
    / | d^* ∈ I_r, Z_{(d^*,frompo rt),(r,top ort)} (y_{(d^*,frompo rt)}) ≠ ∅
    for each (r,toport ) in receivers
        send x - messages (x_{(r,toport )},t) to (r,toport )
        //with input valu e
        //x_{(r,toport )} = Z_{(d^*,frompo rt),(r,top ort)} (y_{(d^*,frompo rt)})
end net - coordinato r
    
```

Fig. 15 Net-coordinator

V.A MODELING TOOL AND CASE STUDY

A. *EASim - Modeling Tool for DSIDs*

A software tool – EASim, was designed and implemented, as

Fig.16, which provides the ability and agility to deal with complex issues of real world, by supporting DSIDs further for analytical modeling.

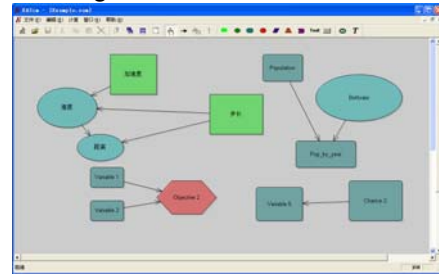


Fig. 16 EASim-software tool for DSIDs modeling

In EASim,

- ◆ The hierarchy description makes it more simplified to build or manage big model and increases the ability for analytical model’s building, organizing and evaluating.
- ◆ And variables can also be vector array except scalar. It’s another source of flexible and abstract ability for model maker. It will redound to make some treat-off among model particular, evaluating time, available data and dimensionality space.
- ◆ To improve representation of discrete processes, EASim not only samples at each evaluating, but also samples at every steps in each evaluating, and provides several statistical methods for analyzing.
- ◆ A script language, Python, is embedded in EASim; and extended by C++ to provide more power for analytical modeling.

In addition, the DSIDs evaluation may include vast data and complex process, especially for complex military SoS counterwork. So, EASim’s evaluating engine is not to immit all correlative data of the model into memory, but to storage model using XML format files, and then respectively evaluate these files by pretreating them to multi-batches. It not only improves running efficiency of evaluating, but also relaxes strict memory and computing power requirements to PC – analysis is often carried out in a combinatorial space of all factors’ various values and common needs to be performed just by PC.

B. *DSIDs Model of Armada Area Defense Issue*

An armada area defense issue is taken for DSIDs modeling example. The basic scenario is that:

- ◆ Attacking planes, from different batches, pierce through the defense lines and then fires cruise missiles to attack weapon carriers of defending side for anti-ship missile intercepting;
- ◆ Attacking side fires some ballistic missiles to attack kernel target directly at opportune time;
- ◆ Defending side intercepts the attacking planes and missiles by air-to-air battles and air defense missiles.

Fig.17 shows the macrocosm structure of the DSIDs model and the influences of factors between time nodes and other nodes, for armada area defense issue.

Fig.18 shows the gross num vs. useable num of node

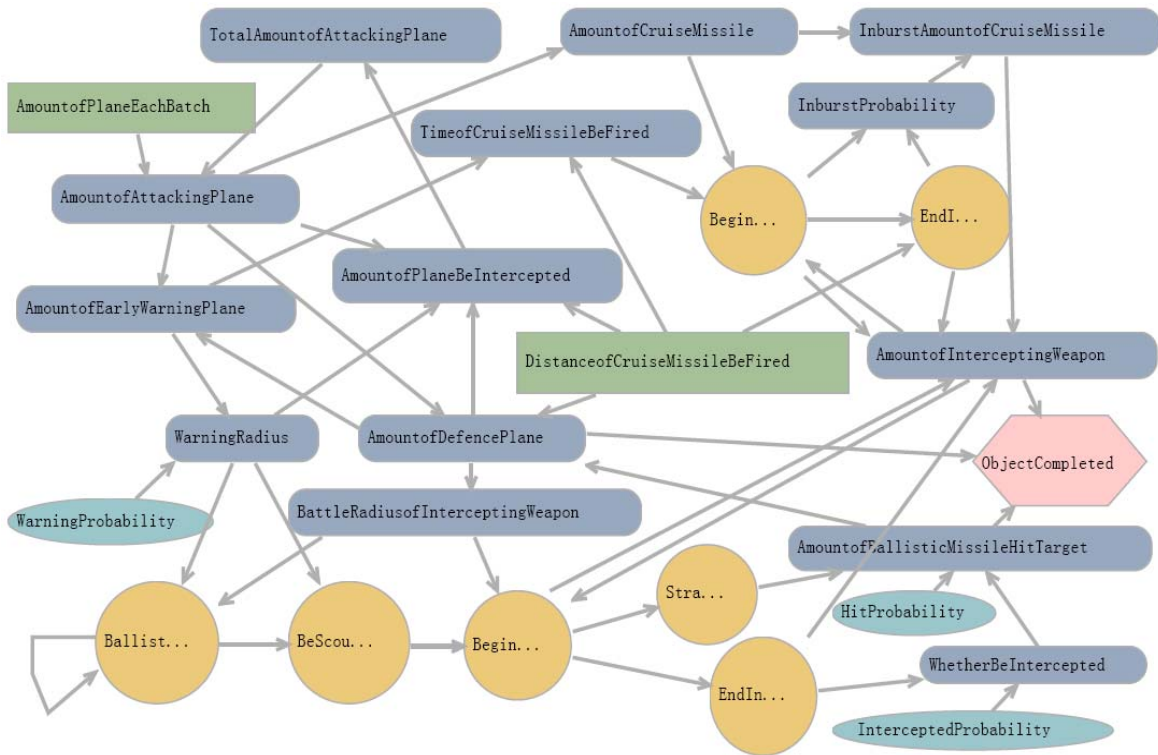


Fig. 17 A reduced version of DSIDs model for armada area defense

'AmountOfInterceptingWeapon' in the DSIDs model. It illustrates that the competition of war resources could come forth at any moment and this could influence the actual occurrences of events.

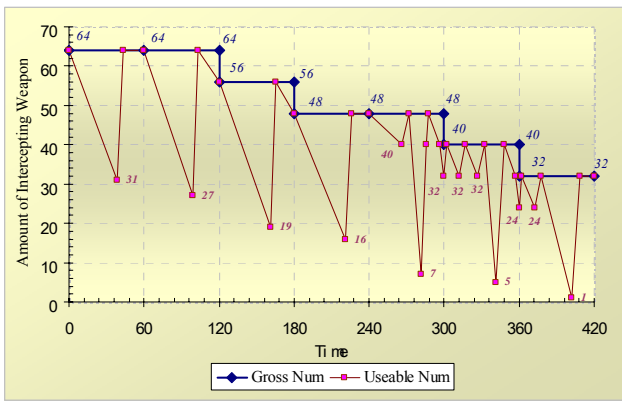


Fig. 18 Gross vs. useable amount of missile intercepting weapons

Fig.19 shows the occurred time of typical events in the DSIDs model. It illustrates that the campaign processes and events them contained could be advanced well, and exhibits the influences that DSIDs could described.

### VI. CONCLUSION

Classic IDs is a good tool to support decision-making for its laconic graphics and effectual approximate reasoning. And the extended Time-sliced IDs has been used for strategic planning successfully. To get more creditability for special object, the weapon and equipment system of systems (SoS) demonstra-

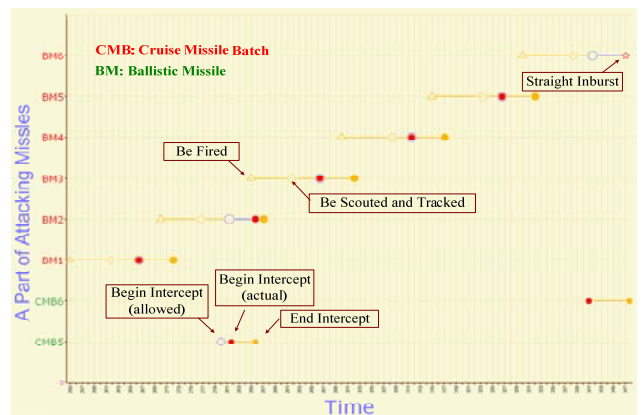


Fig. 19 Occurred time of typical events in the DSIDs model

tion, one of strategic planning issues, the shortcoming of TSIDs is discussed and has been enhanced to own more capability to describe more details of battle processes for influence factors analysis. The proposed class of model is named Dynamic-Stochastic Influence Diagrams (DSIDs). And its modeling formalism and simulation algorithm was described amply. It had been used in the martial planning example excellently. To make the new formalism could be used widely, more work have to do further. For example, as a combination of TSIDs and DES M&S, DSIDs has relationships with DBNs, DBNs, colored Petri nets, and Event Graphs etc, the conversions to these interrelated systems make it's possible to use a variety of analysis algorithms developed for them.

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